



Najważniejsza funkcja na świecie

Andrzej Dąbrowski
Wrocław



Leopold Kronecker
1823-1891

Funkcję ...stworzył dobry Bóg
człowiek zaś nauczył się sprawnie używać funkcji ...

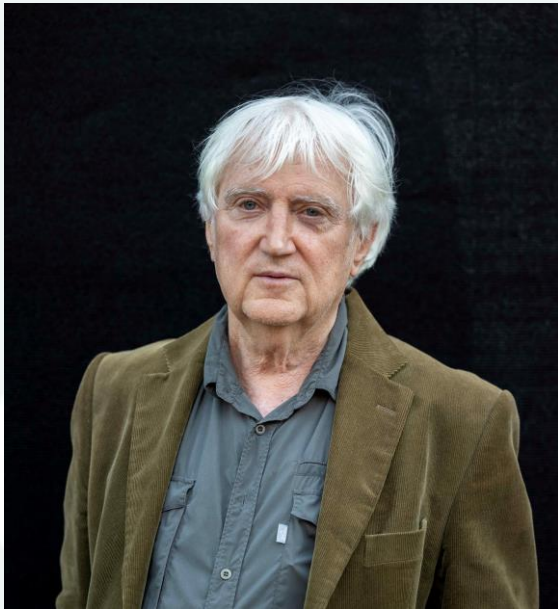






Indianie Munduruku
7000
Amazonia

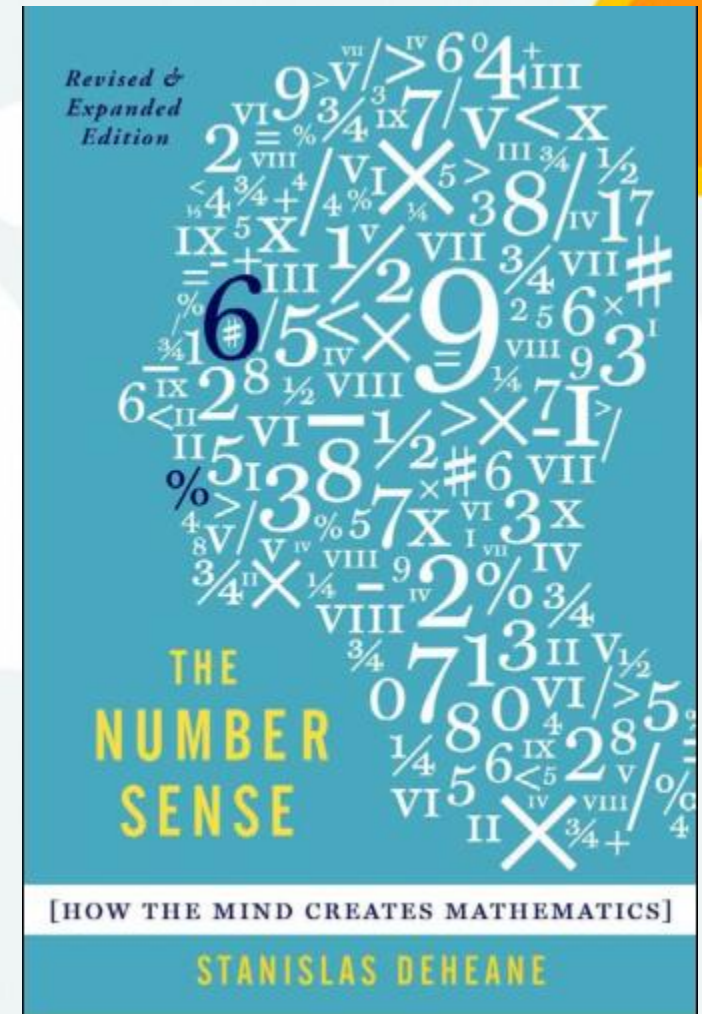


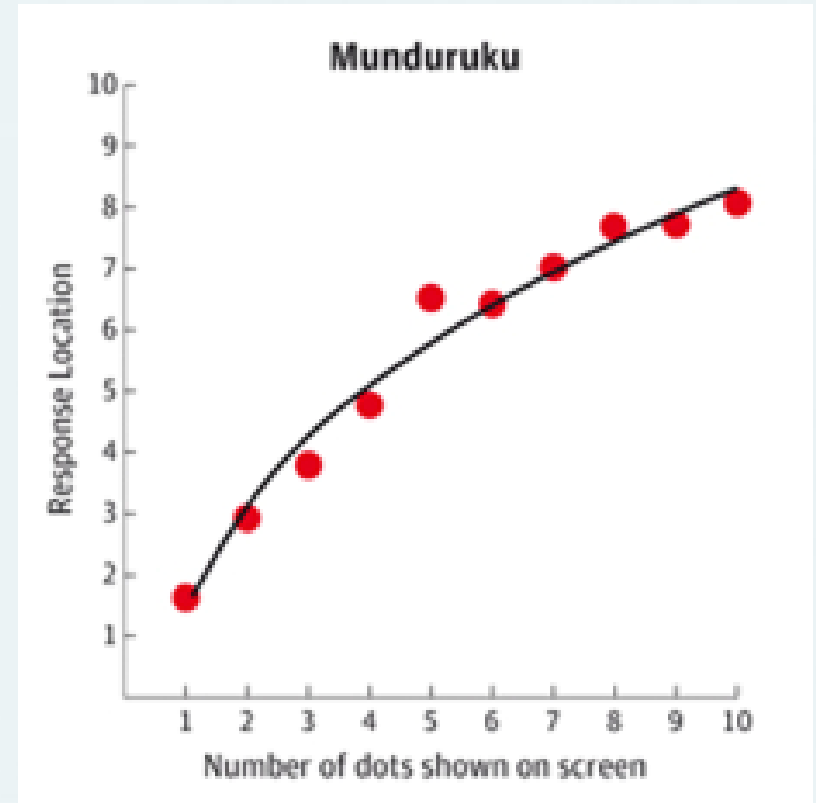
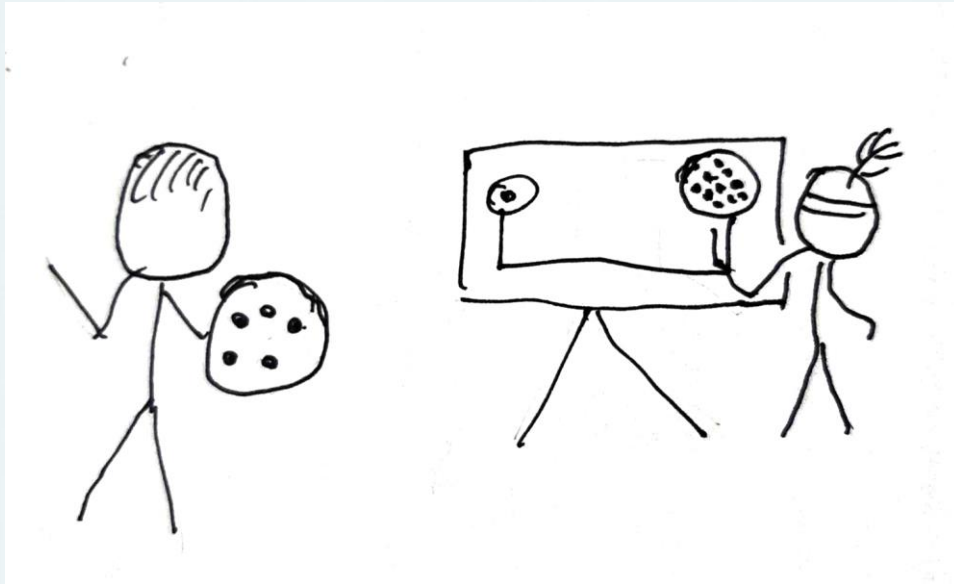
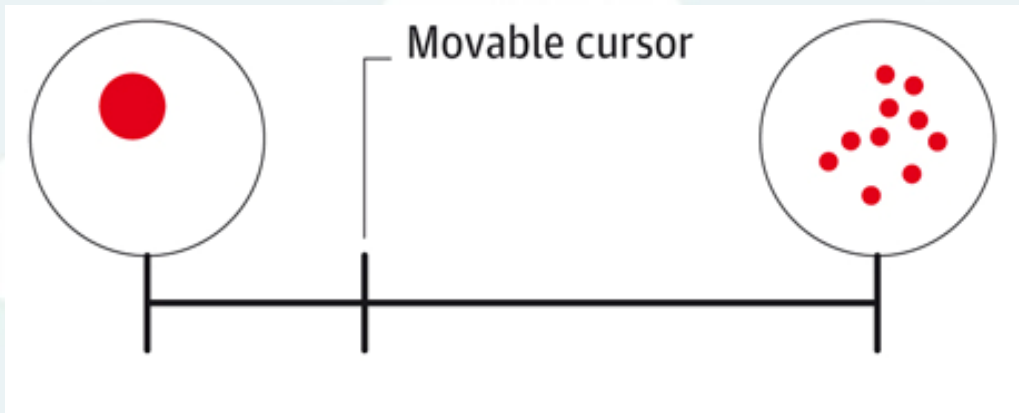


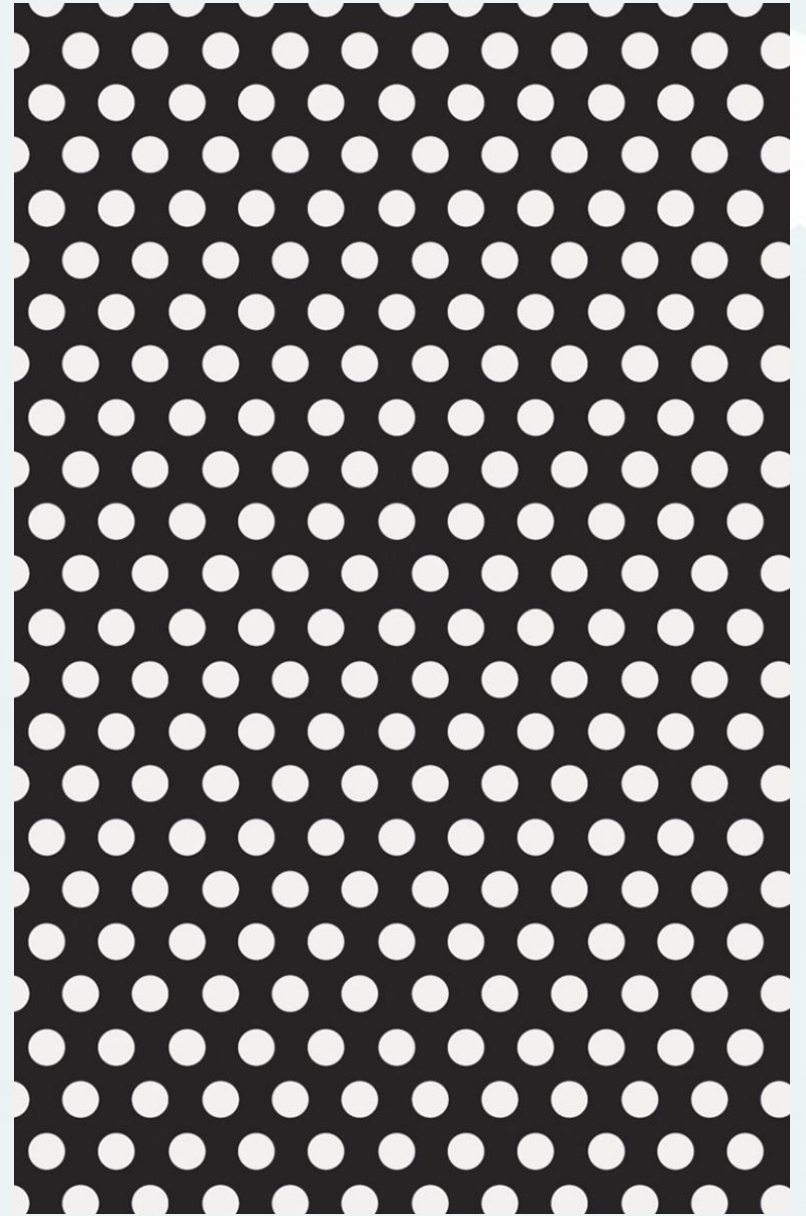
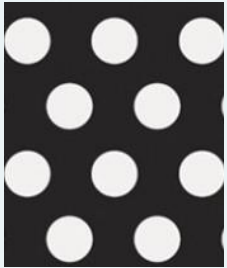
Pierre Pica
prof. CNRS
lingwistyka teoretyczna

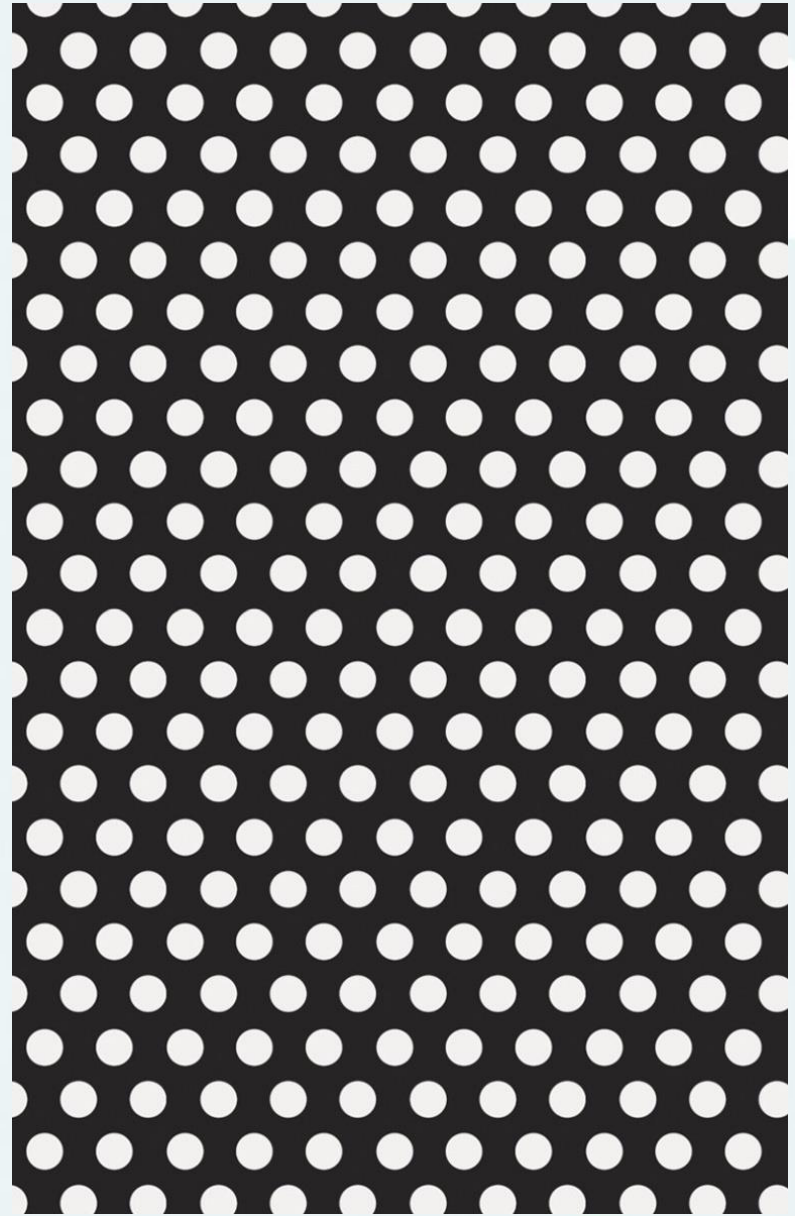
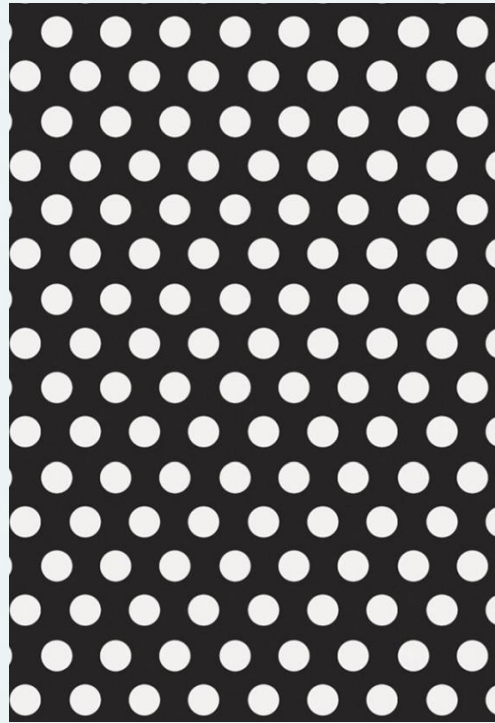
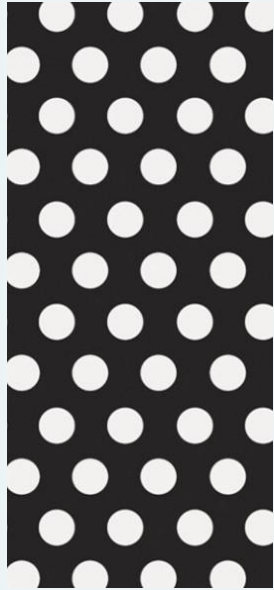
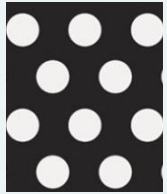


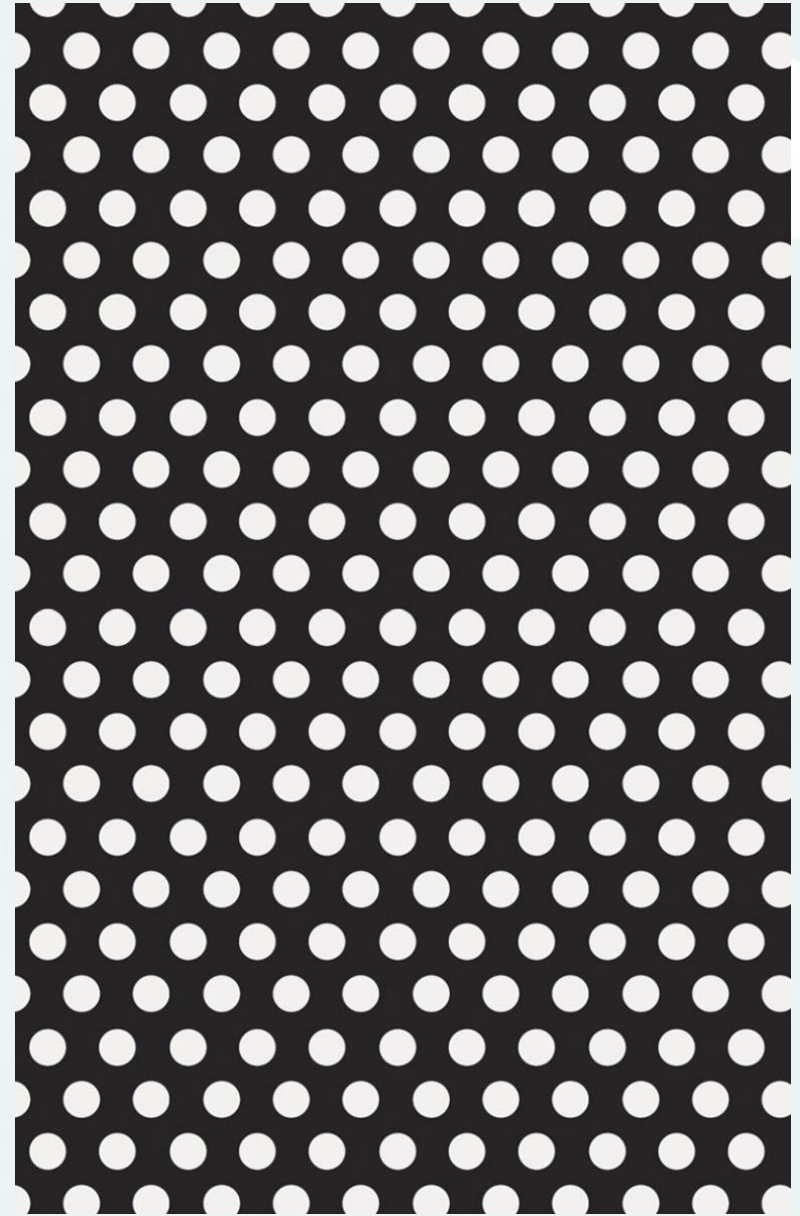
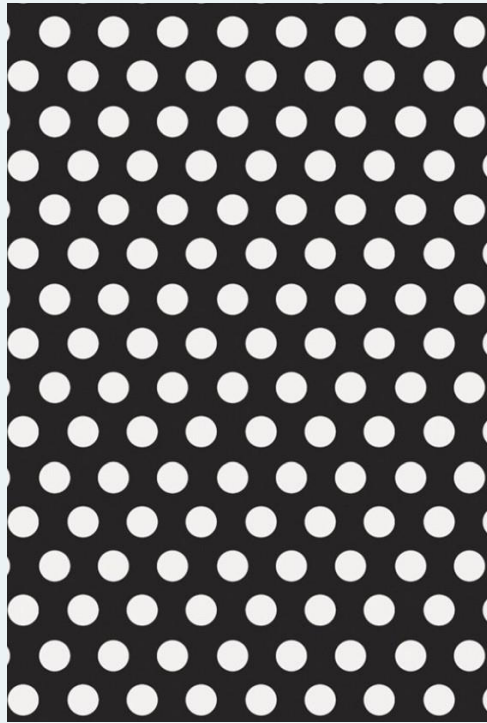
Stanislas Dehaene
Collège de France
Matematyka, neuronauka

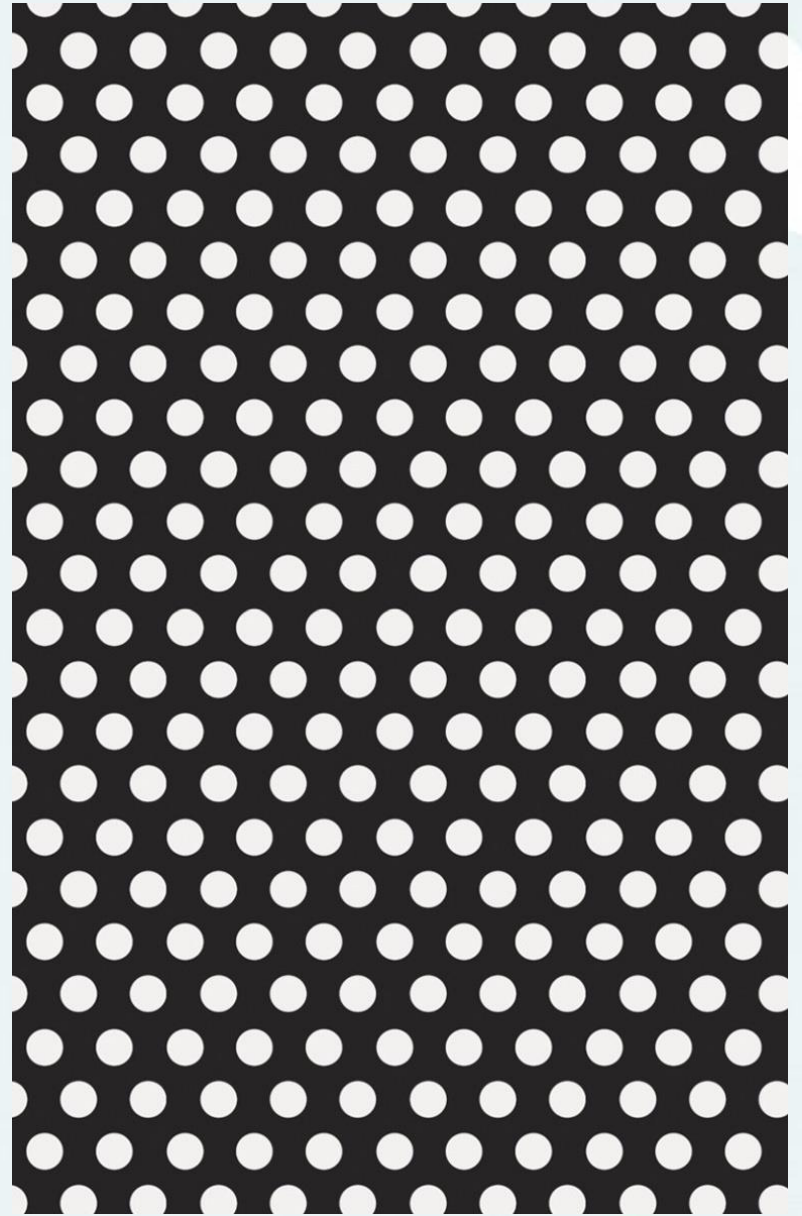
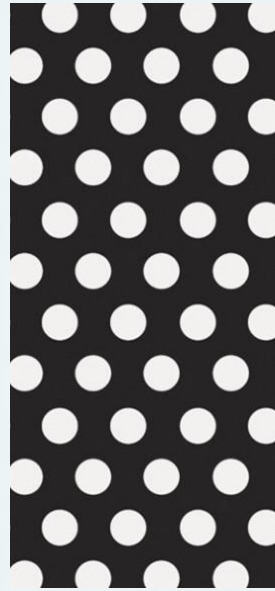
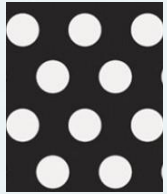














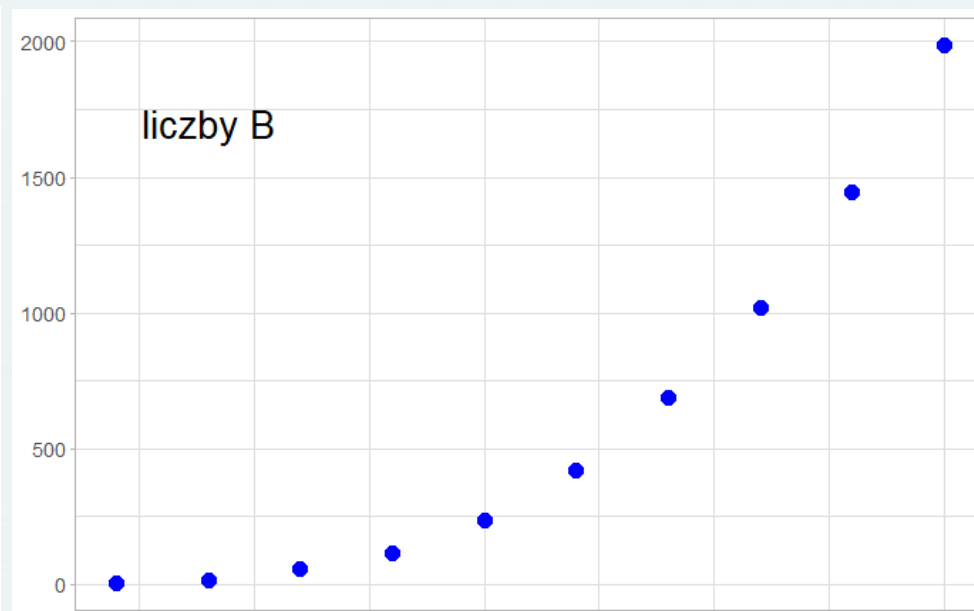
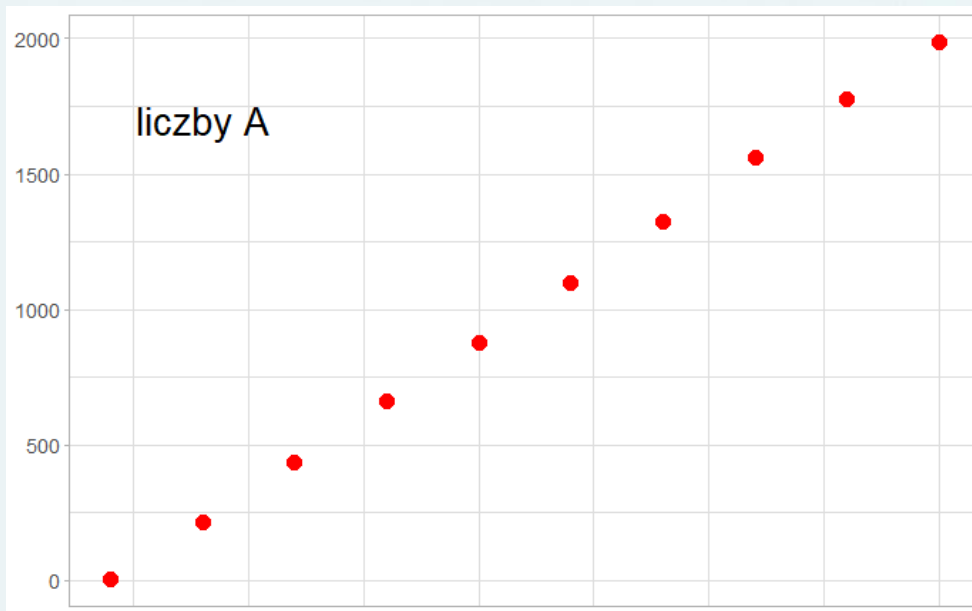






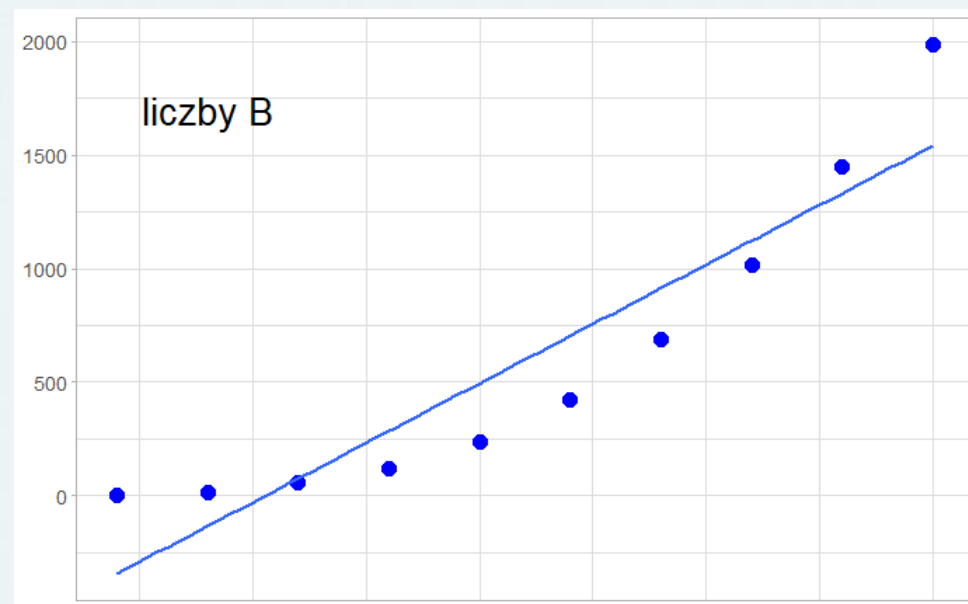
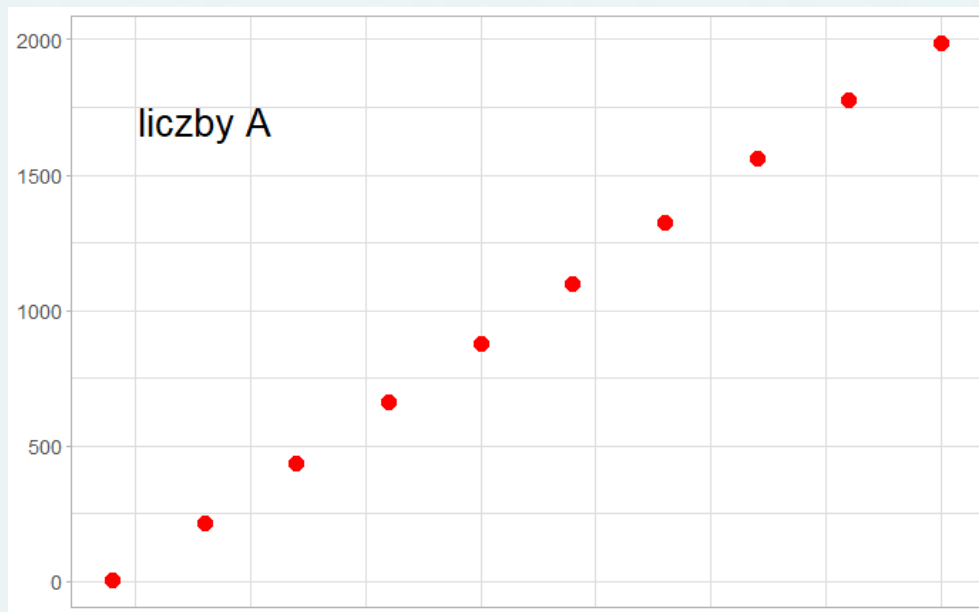
A	87 9	5	132 2	198 7	21 2	177 6	156 1	43 7	1098	663
B	23 8	5	689	198 7	16	144 6	101 8	58	421	117

Które liczby: A czy B
są bardziej równomiernie rozmieszczone
między 0 i 2000?



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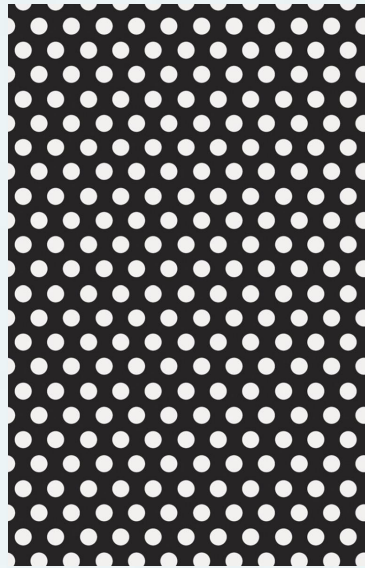
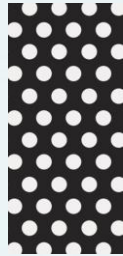
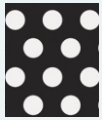




1

3

9



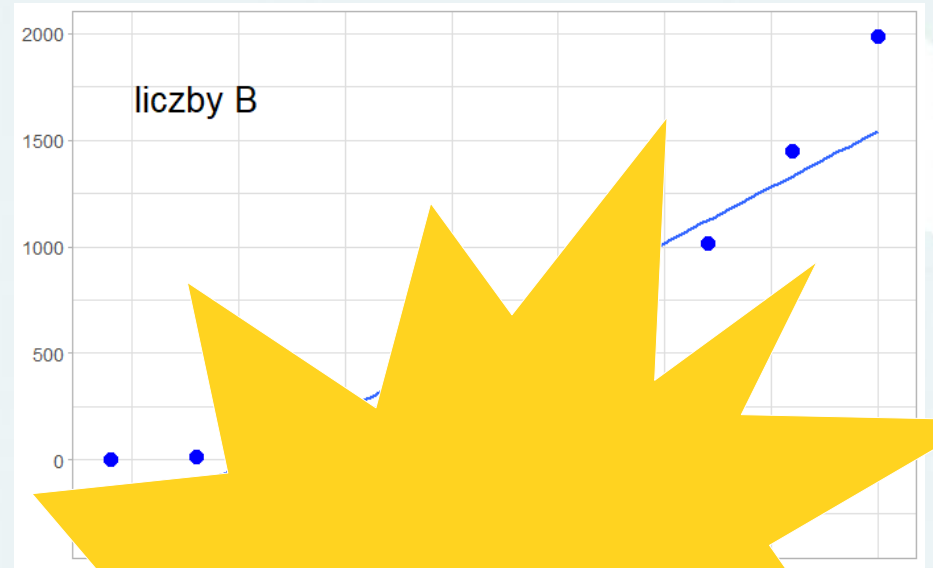
10

50

250

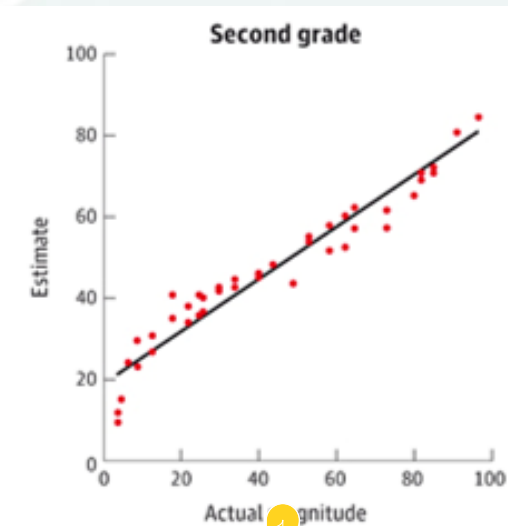
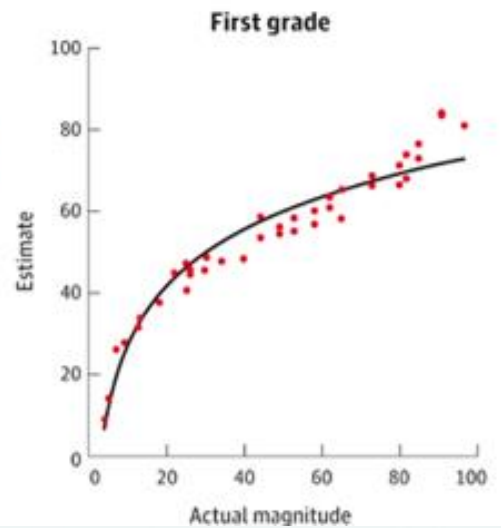
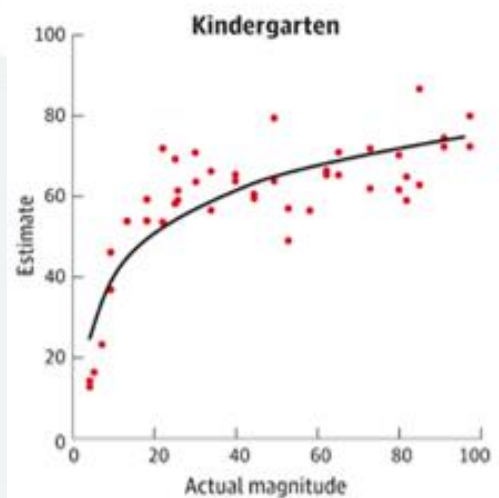
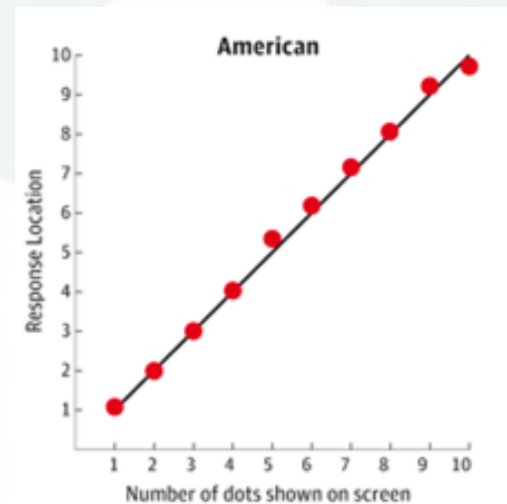
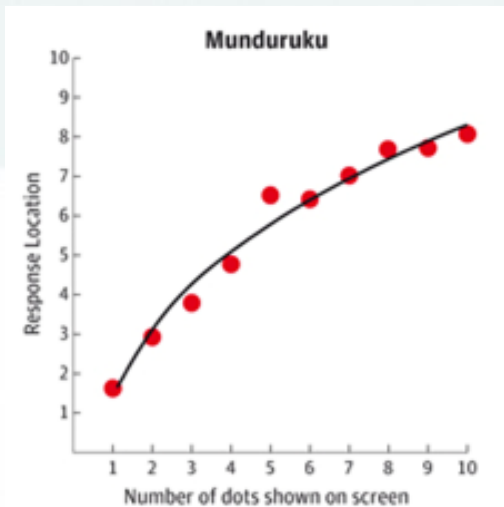
$$y/x = z/y$$

$$\log(y) - \log(x) = \log(z) - \log(y)$$



Proporcja !!





Funkcję **logarytm** stworzył dobry Bóg
człowiek zaś nauczył się sprawnie używać funkcji **liniowej**

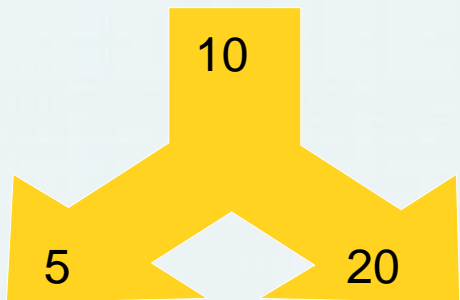


1			10			100			1000
	2	5		20	50		200	500	

1795 Rewolucja Francuska – dziesiętny system metryczny.

Główne jednostki: 1, 10, 100, 1000, ...

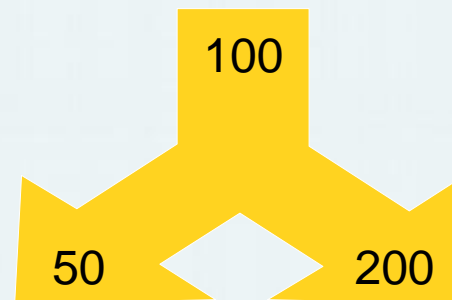
Jednostki pośrednie są podzieleniem/pomnożeniem jednostki głównej przez 2



$$10 \cdot 2 = 20$$

$$20 \cdot 2.5 = 50$$

$$50 \cdot 2 = 100$$





Plk. Charles Renard
1847 - 1905

1877 Liczby Renarda (liczby normalne) → ISO
Minimalny błąd względny

System **R_n**:

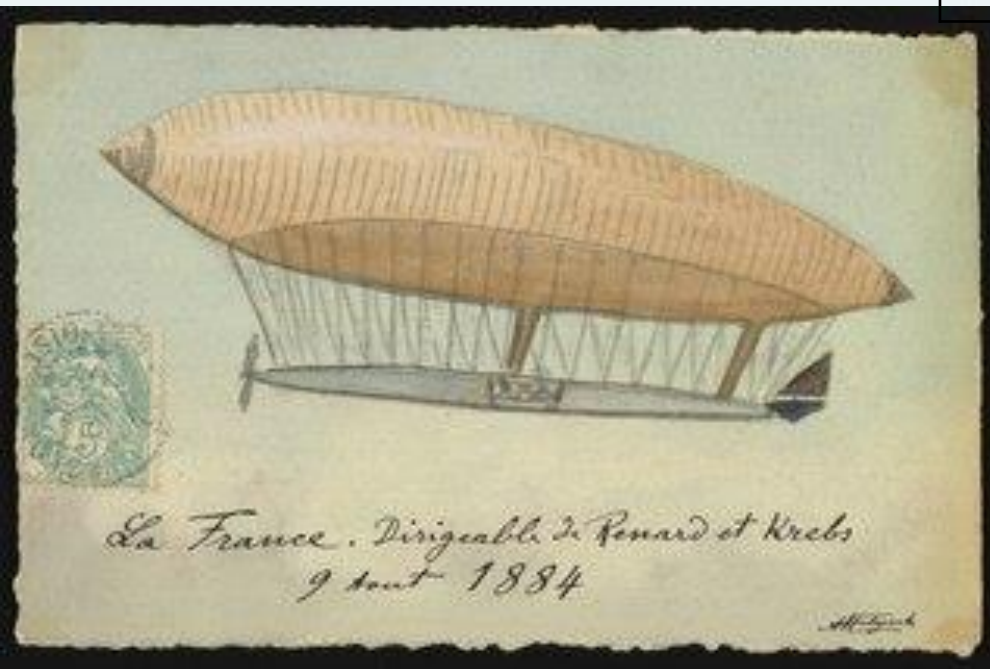
1 – 10 na n proporcjonalnych odcinków

R₅

0	1	2	3	4	5	6
1,00					10,0 0	
q^0	q^1	q^2	q^3	q^4	q^5	q^6

$$q=10^{1/5} \approx 1,5850$$

Redukcja rodzajów lin balonowych z 425 do 17



n	1	2	3	4	5	6	7	8	9	10	11
$10^{n/5}$	1,58	2,51	3,98	6,31	10,00	15,85	25,12	39,81	63,10	100,00	158,49
R5	1,6	2,5	4	6,3	10	16	25	40	63	100	160

Šrubby 5mm – 50 mm

R5	1,6	2,5	4	6,3	10	16	25	40	63	100	160
----	-----	-----	---	-----	----	----	----	----	----	-----	-----



2		4		8		16		32
	2,828		5,657		11,314		22,627	

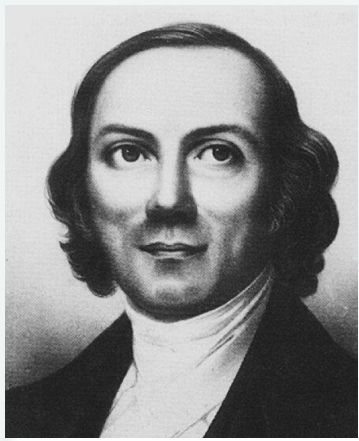
$$q = \sqrt{2} \approx 1.4142$$

$$2 * q = 2,828 = 4/q \quad 4 * q = 5,657 = 8/q \quad 8 * q = 11,314 = 16/q$$

10	12	15	18
22	27	33	39
47	56	68	82

$$R12 (E12) \quad q = 10^{1/12} \approx 1,2115$$



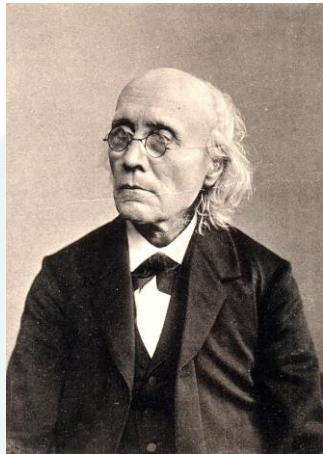


Ernst Heinrich Weber
(1795–1878)
fizjolog i anatom



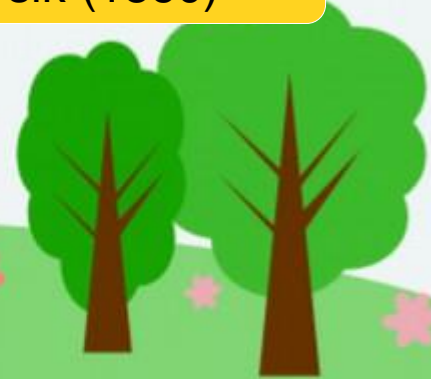
$$\Delta p = c \cdot \Delta s / s$$

$$p'(s) = c/s$$
$$p(s) = \log(s/s_0)$$



Gustav Theodor Fechner
(1801- 1887)
fyzyk, filozof i psycholog

Prawo Webera-Fechnera
Elemente der Psychophysik (1860)



Prawo Webera - Fechnera na co dzień

$$\text{decybel} = 20 \log_{10}(p/p_{\text{ref}})$$

p – średnie odchylenie ciśnienia atmosferycznego

p_{ref} - wartość progowa dla normalnie słyszającej osoby, odpowiadająca

Pokrętko głośności w radio działa logarytmicznie

10 dB – szelest liści przy łagodnym wietrze

20 dB – szept

60 dB – odkurzacz (100 * szept)

90 dB – ruch uliczny (3000 * szept)

300 dB – (szacowane, 100 m) wybuch wulkanu Krakatau w Indonezji w 1883 r. Prawdopodobnie



Prawo Webera - Fechnera na co dzień

$$\text{decybel} = 20 \log_{10}(p/p_{\text{ref}})$$

$$\text{PH} = - \log_{10}([\text{H}^+])$$

[H⁺] stężenie jonów wodorowych w molach na litr

Cytryna 2
Pomarańcza 4
Woda 7



Prawo Webera - Fechnera na co dzień

$$\text{decybel} = 20 \log_{10}(p/p_{\text{ref}})$$

$$\text{pH} = - \log_{10}([\text{H}^+])$$

$$M = \log_{10}(A/A_0)$$

Skala Richtera

A – maksymalne odchylenie seismografu

A₀ – parametr zależny od odległości od epicentrum

M > 8 zdarzają się raz na rok

M = 9.5 Wielkie trzęsienie w Chile 1960



Prawo Webera - Fechnera na co dzień

$$\text{decybel} = 20 \log_{10}(p/p_{\text{ref}})$$

$$\text{PH} = -\log_{10}([\text{H}^+])$$

$$M = \log_{10}(A/A_0)$$

Obserwowana wielkość gwiazdowa

$$m = -2,5 \log_{10}(J/J_V)$$

J jasność gwiazdy

J_V jasność Vega

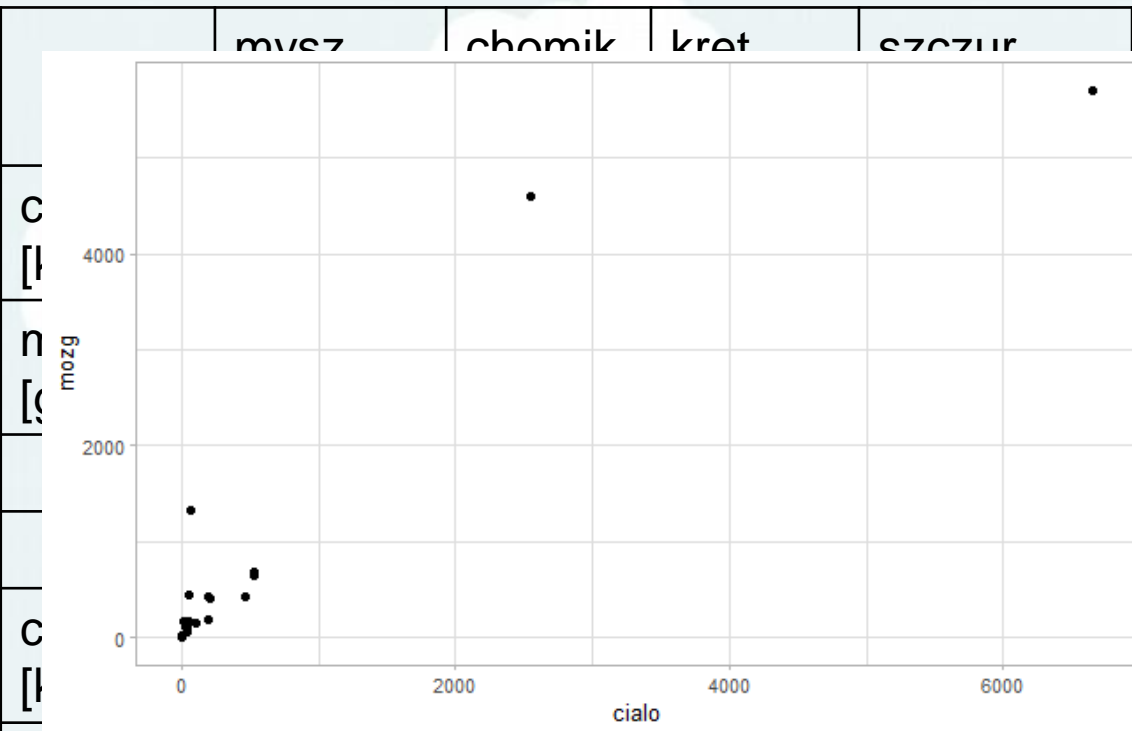
$m = 1, \dots, 6$ wielkości gwiazdowe Klaudiusza Ptolemeusza (100-170)

$m = -4,2$ Wenus (48 razy jaśniejsza niż Vega)

$m = -26,83$ Słońce

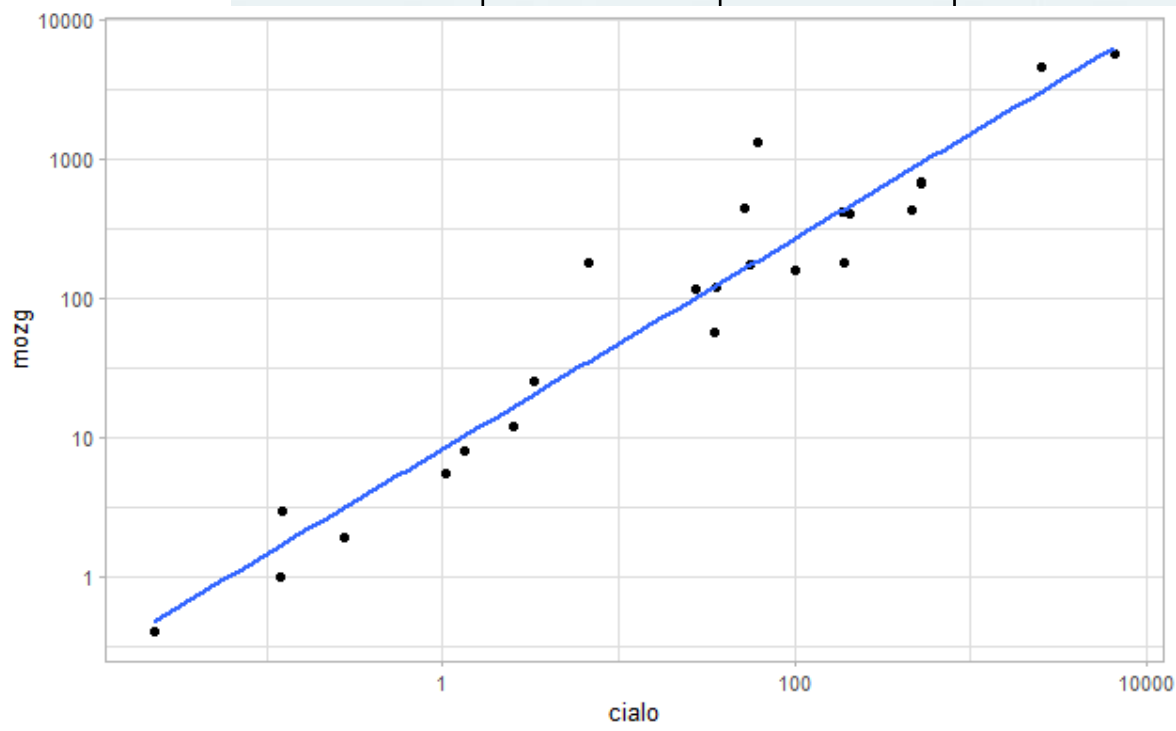
$m = 31.05$ najdalszy obiekt w teleskopie Hubble'a

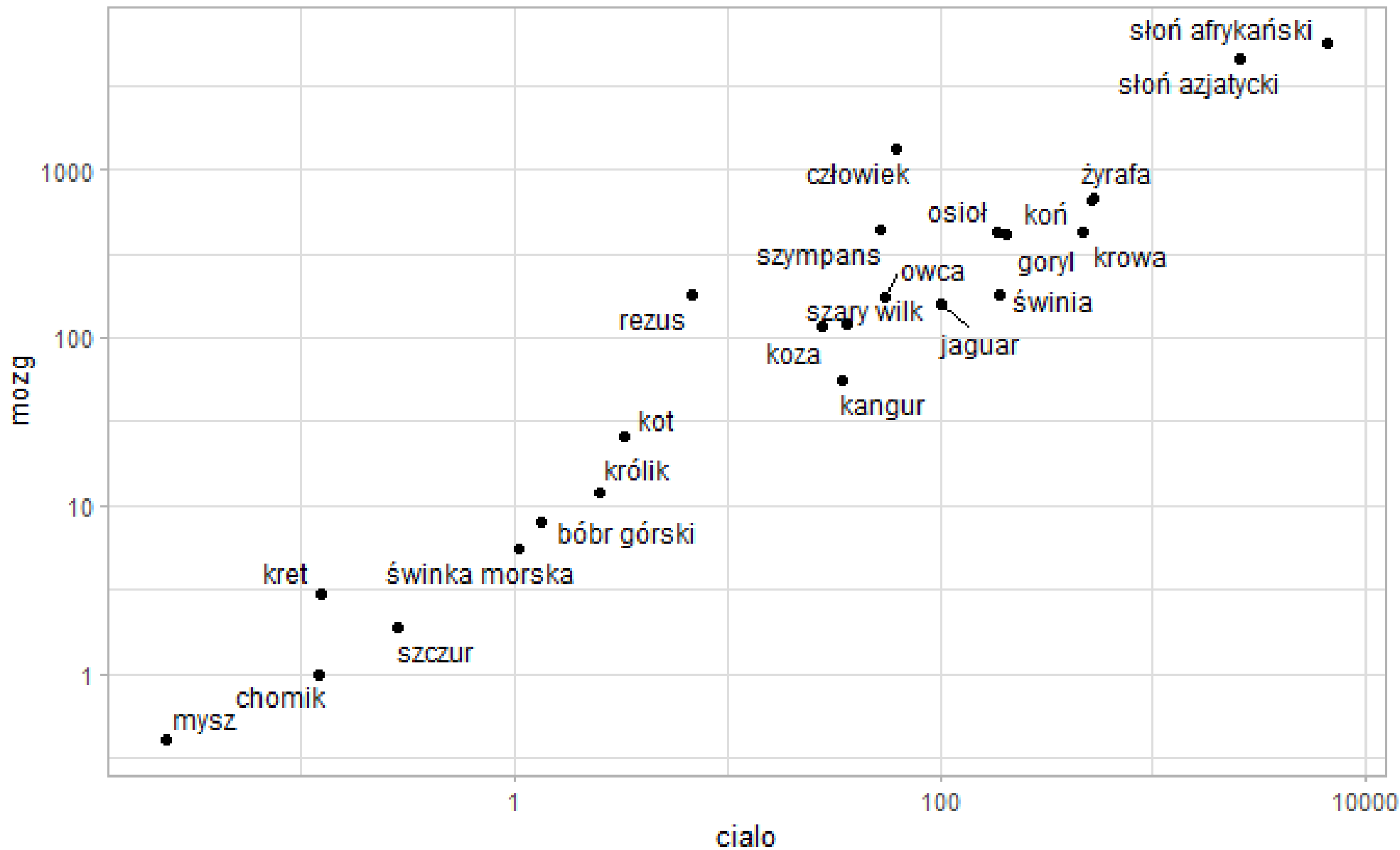




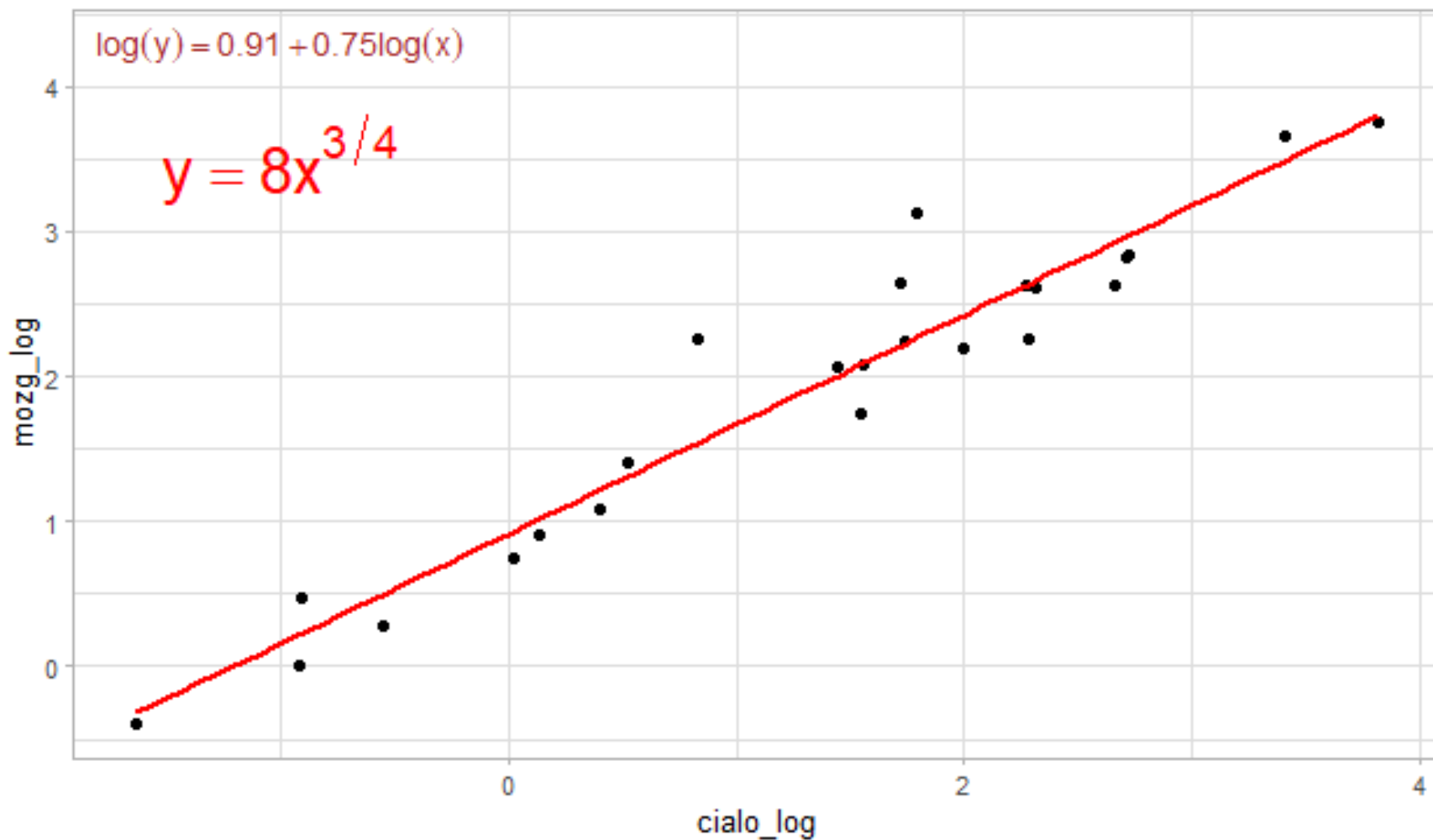
świnka morska	bóbr górski	królik	kot
1,04	1,35	2,50	3,30
5,50	8,10	12,10	25,60
szympan	owca	człowiek	jaguar
52,16	55,50	62,00	100,00

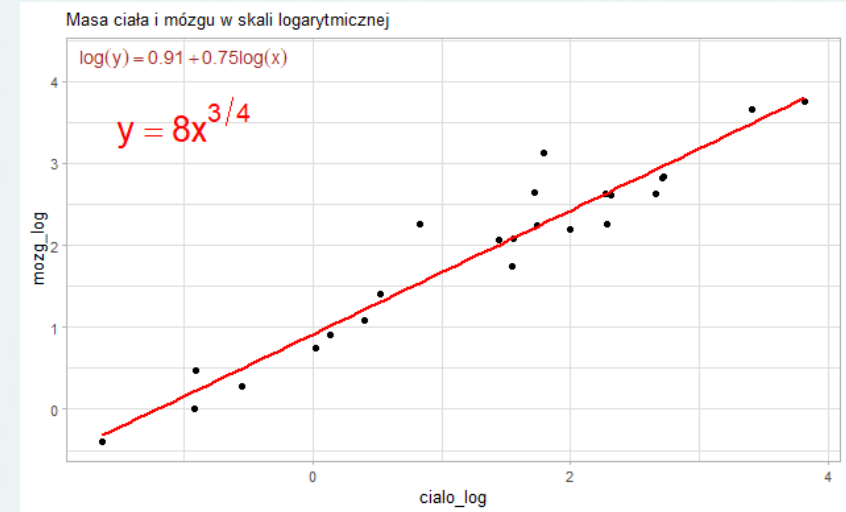
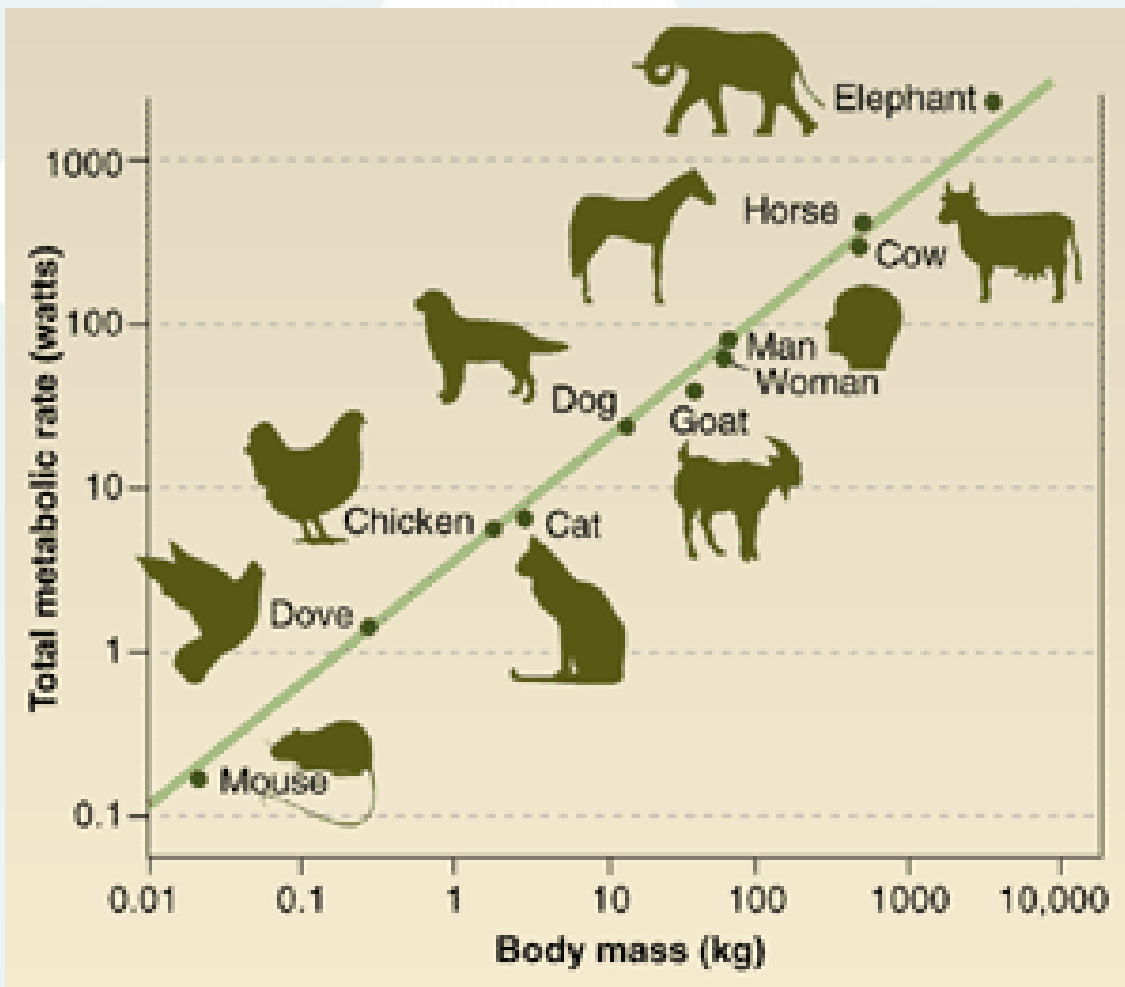
mozg [g]	179,00	115,00	56,00	1
	osioł	świnia	goryl	kr
ciało [kg]	187,10	192,00	207,00	46
mozg [g]	419,00	180,00	406,00	42





Masa ciała i mózgu w skali logarytmicznej



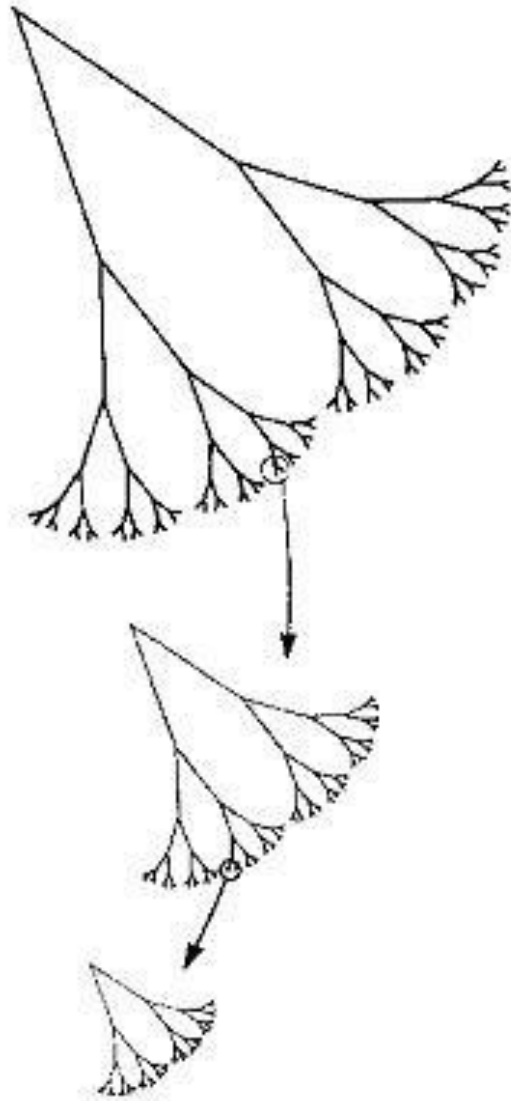


Prawo Kleibera
 $y = c x^{3/4}$

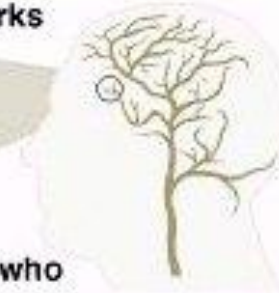
Dlaczego nie
 $y = c x^{2/3}$?



Self-Similar Structure (Fractal)



The Networks



The scientists who developed the scaling theory took clues from naturally occurring networks that carry life-sustaining fluids in organisms in which each small part is a replica of the whole. No matter how big the organism, the ends of these fractal networks are always the same size, since individual cells are of similar size in all organisms.

CIRCULATORY
SYSTEM

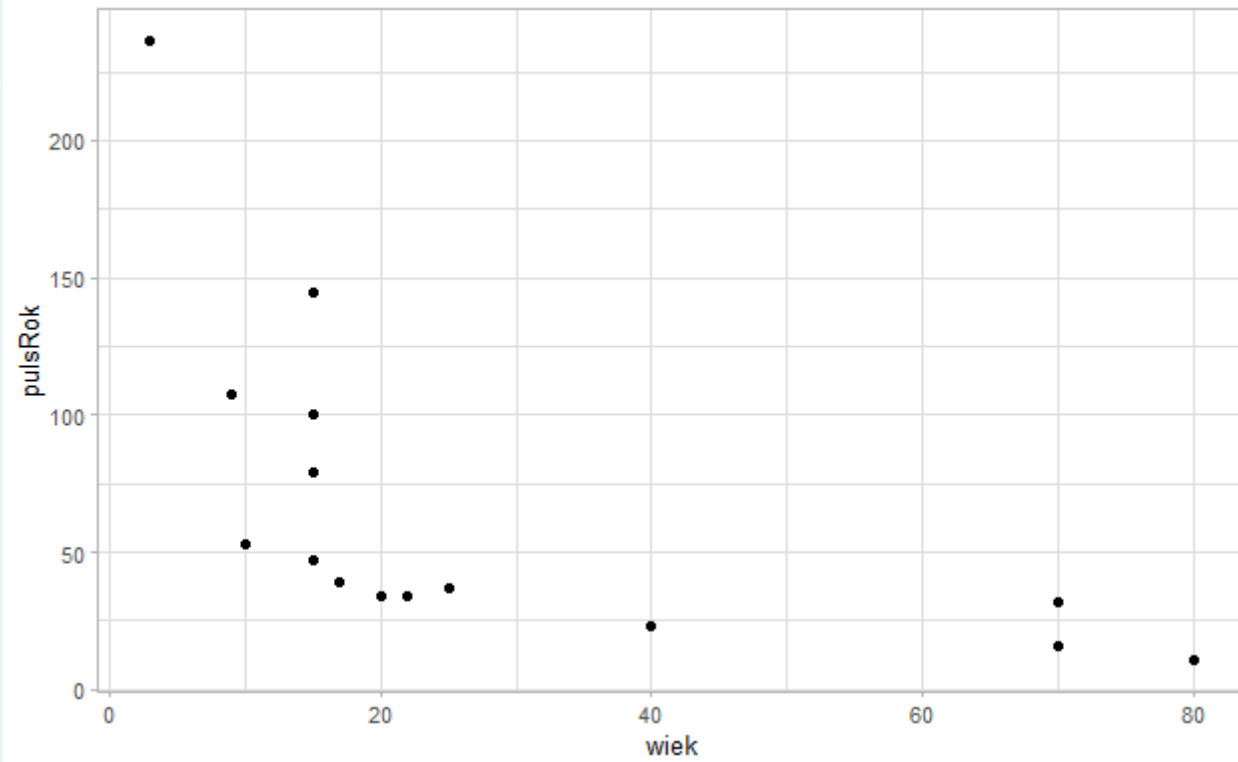


LUNGS



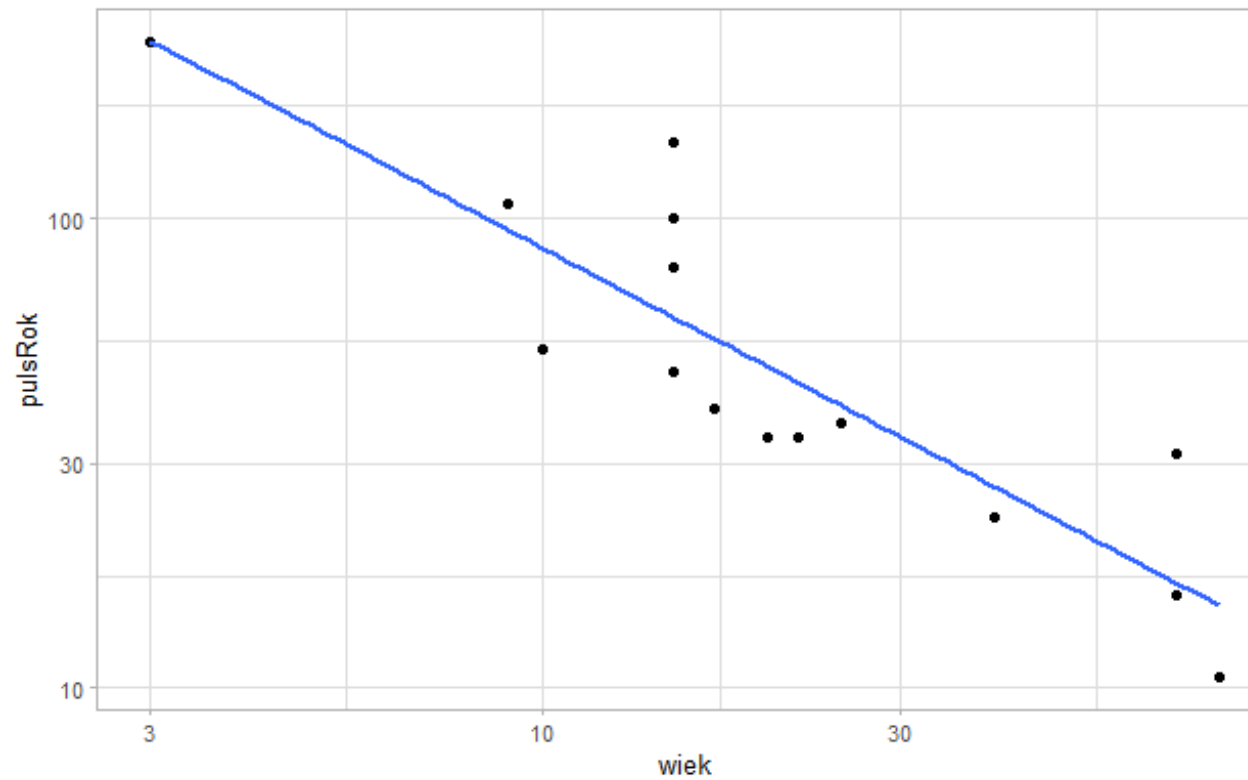
TREE BRANCHES

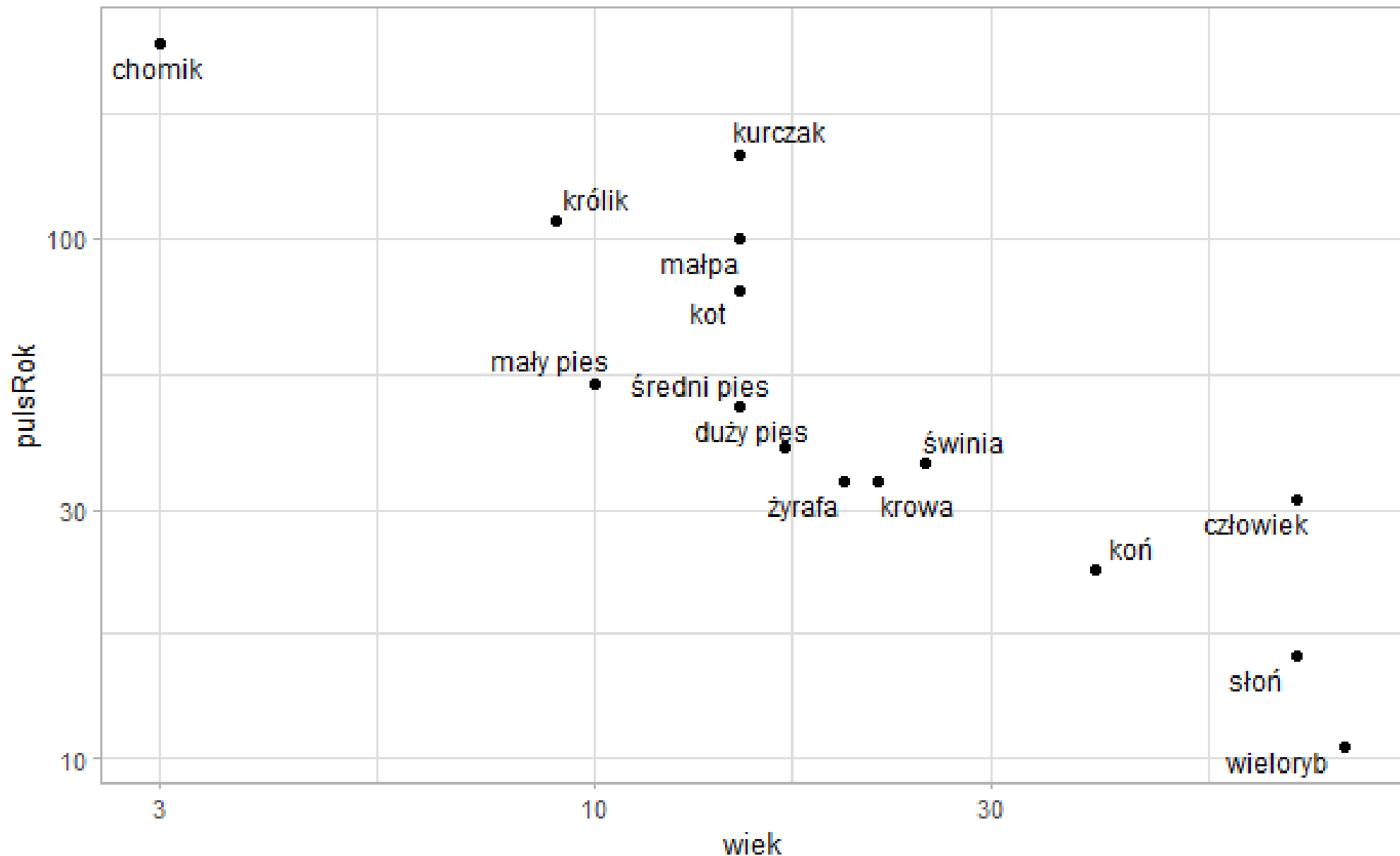




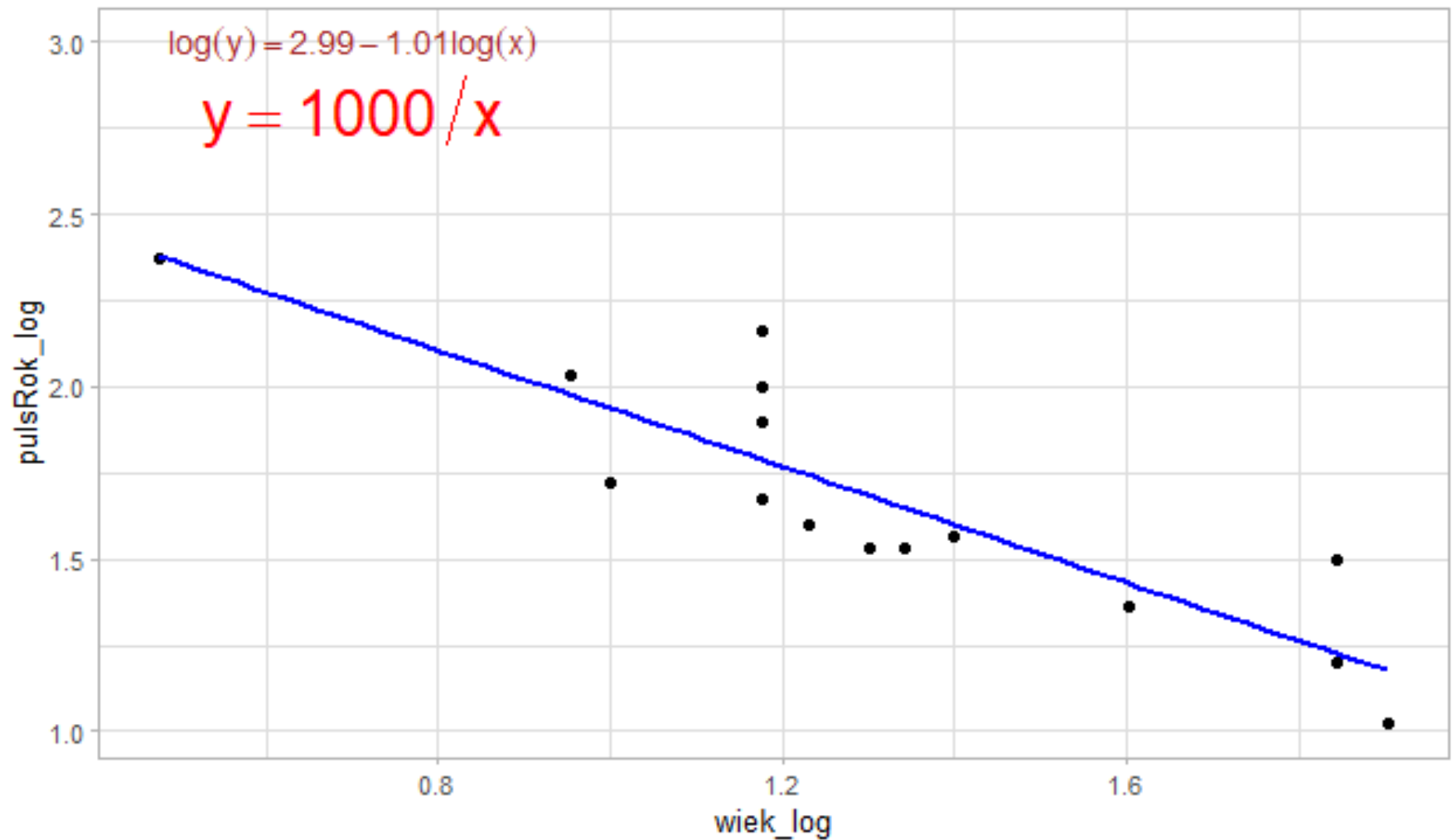
	chomik	kurczak	małpa
75	450	275	190
69	237	145	100
7	3	15	15
łoś	żyrafa	wieloryb	
60	65	20	
6	34	11	

[min]			
wiek [lata]	40	22	25





Wiek i pulsy/rok w skali logarytmicznej



$\text{pulsRok} = 1000 / \text{długość życia}$

Liczba pulsów w całym życiu = długość życia * pulsRok = 1000 mln = **miliard**



Similarity in the number of lifespan heartbeats among non-hibernating homeothermic animals.

Livingstone SD, Kuehn LA.

Abstract

An investigation was made of the available data on heart rates and maximum lifespan of a number of vertebrates from a variety of sources; only data pertinent to resting adult non-anesthetized homeothermic mammals and birds in a state of thermal neutrality were subsequently analyzed. All known hibernators were excluded because of their extreme, and largely unknown, range of heartbeat from season to season. Plots of heart rate (beats per minute) against reciprocal of lifespan in years showed surprisingly good fits ($r = +0.90$ for mammals and $r = +0.64$ for birds). Computation of the total number of heartbeats in the maximum recorded lifespans of the mammalian and avian species involved in this study showed that the mean cumulative heartbeat number for 31 mammalian species was $100 \pm 8 \text{ S.E.M.} \times 10(7)$ beats and for 23 avian species was $326 \pm 22 \text{ S.E.M.} \times 10(7)$ beats. This paper documents this analysis, which supports the concept of a close similarity in lifespan heartbeats among mammalian species and among avian species.

PMID: 518447

Ssaki: 1 miliard pulsów w życiu
Ptaki: 3 miliardy pulsów w życiu





Low income countries

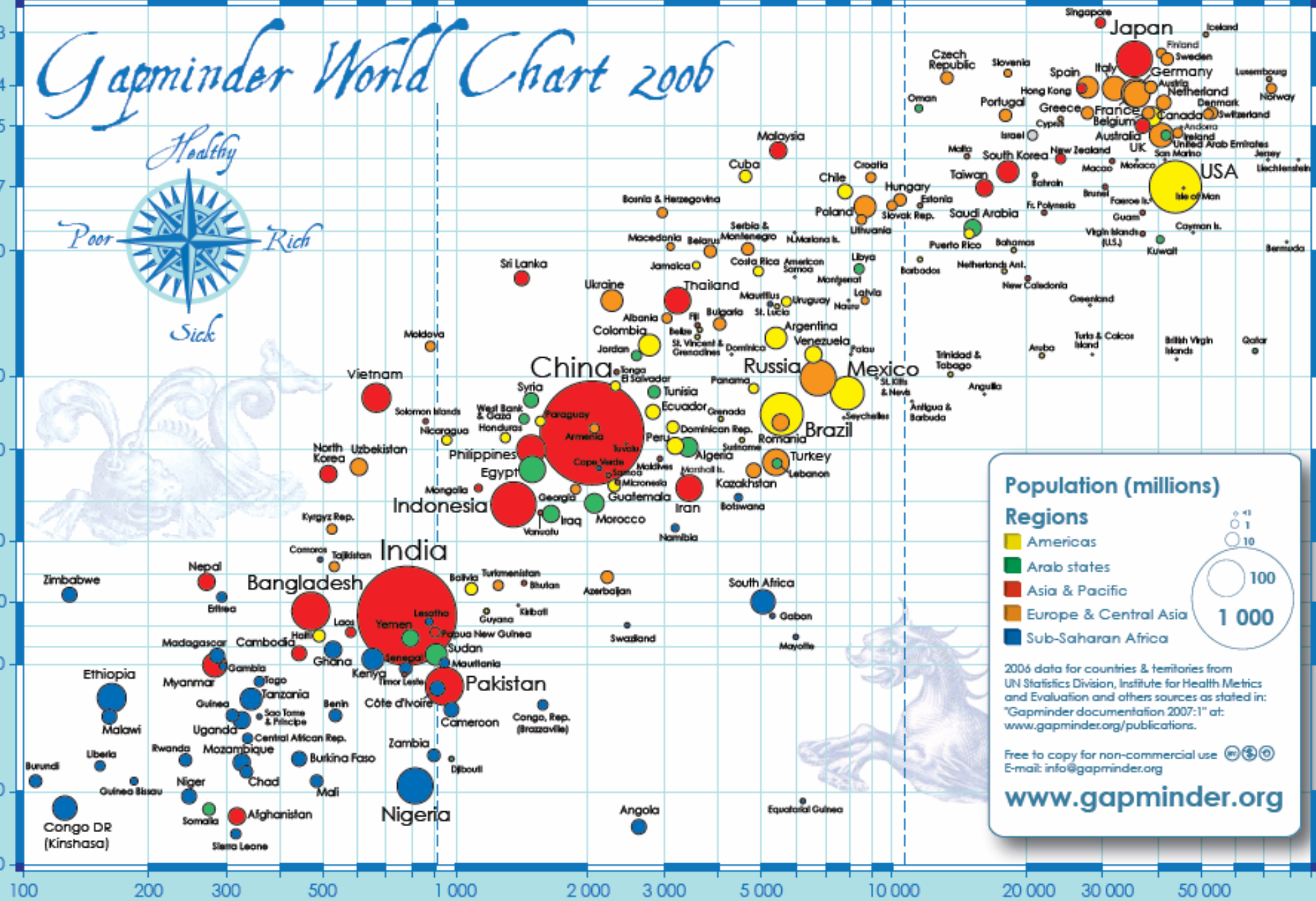
Middle income countries

High income countries

Gapminder World Chart 2006

Children dying before age 5 per 1000 live births (log)

Health



Population (millions)

Regions

- Americas (Yellow)
- Arab states (Green)
- Asia & Pacific (Red)
- Europe & Central Asia (Orange)
- Sub-Saharan Africa (Blue)

Population size legend:
 ○ 1
 ○ 10
 ○ 100
 ○ 1000

2006 data for countries & territories from UN Statistics Division, Institute for Health Metrics and Evaluation and other sources as stated in: "Gapminder documentation 2007:1" at: www.gapminder.org/publications.

Free to copy for non-commercial use
 E-mail: info@gapminder.org

www.gapminder.org

Money

Gross National Income per capita - in US dollar by exchange rate (log)

GAPMINDER



